

Please write clearly in block capitals.

Centre number

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Candidate number

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Surname

Forename(s)

Candidate signature

A-level PHYSICS

Paper 2

Wednesday 21 June 2017

Morning

Time allowed: 2 hours

Materials

For this paper you must have:

- a pencil and a ruler
- a scientific calculator
- a Data and Formulae booklet.

Instructions

- Use black ink or black ball-point pen.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- Do all rough work in this book. Cross through any work you do not want to be marked.
- Show all your working.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 85.
- You are expected to use a scientific calculator where appropriate.
- A Data and Formulae Booklet is provided as a loose insert.

For Examiner's Use	
Question	Mark
1	
2	
3	
4	
5	
6	
7	
8–32	
TOTAL	



Kinetic theory model/assumptions:

Section A

VINCE

Answer all questions in this section.

Volume of gas molecules \ll volume of container

0 1 . 1

A number of assumptions are made when explaining the behaviour of a gas using the molecular kinetic theory model.

State one assumption about the size of molecules.

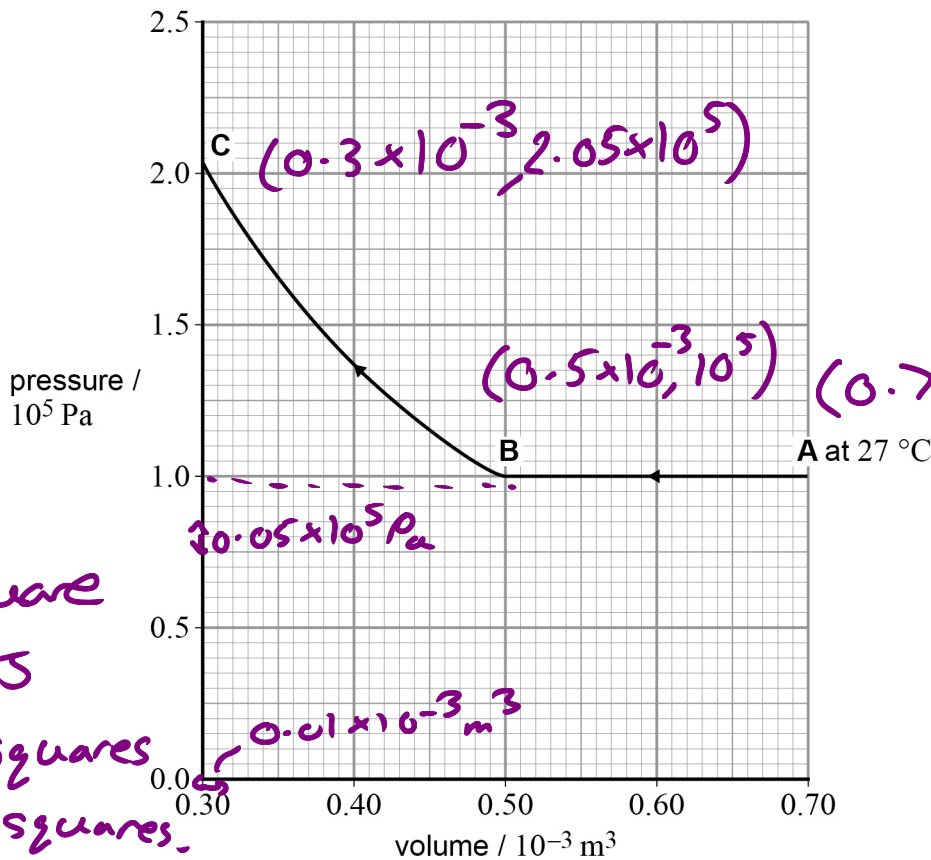
[1 mark]

Volume of the gas molecules is much smaller than the volume of the container.

Figure 1 shows how the pressure changes with volume for a fixed mass of an ideal gas.

At A the temperature of the gas is 27°C . The gas then undergoes two changes, one from A to B and then one from B to C.

Figure 1



Area of one square $\rightarrow 0.05$
 Count squares ~ 170 squares.



T_A in kelvin is $27 + 273 = 300K$

0 1 . 2

Calculate the number of gas molecules trapped in the cylinder using information from the initial situation at A.

$T_A = 27^\circ C =$ ($pV = Nk_B T$) [2 marks]

$p_A = 10^5 Pa$

$V_A = 0.7 \times 10^{-3} m^3$

$N = \frac{pV}{k_B T}$

$N = \frac{10^5 \times 0.7 \times 10^{-3}}{1.38 \times 10^{-23} \times 300} = 1.691 \times 10^{22}$

number of molecules = 1.7×10^{22}

0 1 . 3

Calculate, in K, the change in temperature of the gas during the compression that occurs between A and B.

$pV = Nk_B T$
 $\frac{pV}{T} = Nk_B$
 Fixed mass of gas, N constant

$\frac{p_A V_A}{T_A} = Nk_B = \frac{p_B V_B}{T_B} \rightarrow \frac{T_B}{T_A} = \frac{p_B V_B}{p_A V_A} \rightarrow T_B = \frac{p_B V_B}{p_A V_A} \times T_A$ [2 marks]

$p_A = p_B$
 $T_B = \frac{V_B}{V_A} \times T_A = \frac{0.5 \times 10^{-3}}{0.7 \times 10^{-3}} \times 300 = 214.285 \dots$

$T_B - T_A = 300 - 214.285 \dots = -85.714 \dots \approx -86 K$

change in temperature = $-86 K$

0 1 . 4

Deduce whether the temperature of the gas changes during the compression from B to C.

Isothermal: same temperature [2 marks]

$pV = Nk_B T$, T is constant, N is constant
 Isothermal: $p_B V_B = p_C V_C$

$p_B V_B = 10^5 \times 0.5 \times 10^{-3} = 50 Pa m^3$

$p_C V_C = 2.05 \times 10^5 \times 0.3 \times 10^{-3} = 61 Pa m^3$

$p_B V_B \neq p_C V_C$, so the temperature of the gas changes since the change is not isothermal.

Question 1 continues on the next page

Turn over ►

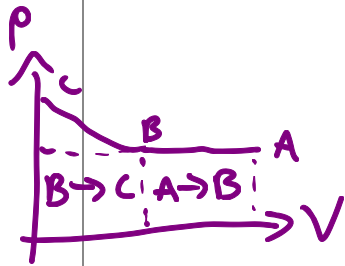


0 1 . 5

Compare the work done on the gas during the change from A to B with that from B to C on Figure 1.

[3 marks]

Work done on gas is the area under the pV graph.



	$V/10^{-3} \text{ m}^3$	$p/10^5 \text{ Pa}$
A	0.7	1
B	0.5	1
C	0.3	2.05

Work done is area under the graph

$A \rightarrow B$: height = 10^5 Pa , length = $(0.7 - 0.5) \times 10^{-3} = 0.2 \times 10^{-3} \text{ m}^3$
Area = $10^5 \times 0.2 \times 10^{-3} = 20 \text{ J}$

$B \rightarrow C$: rectangle: height = 10^5 Pa , length = $(0.5 - 0.3) \times 10^{-3} = 0.2 \times 10^{-3} \text{ m}^3$
Area of rectangle = 20 J

Area between rectangle and curve

$B \rightarrow C$ is $0.05 \times 170 = 8.5 \text{ J}$

Work done from $B \rightarrow C = 20 + 8.5 = 28.5 \text{ J}$

so work done from $B \rightarrow C$ is greater than the work done from $A \rightarrow B$ by 8.5 J .



Turn over for the next question

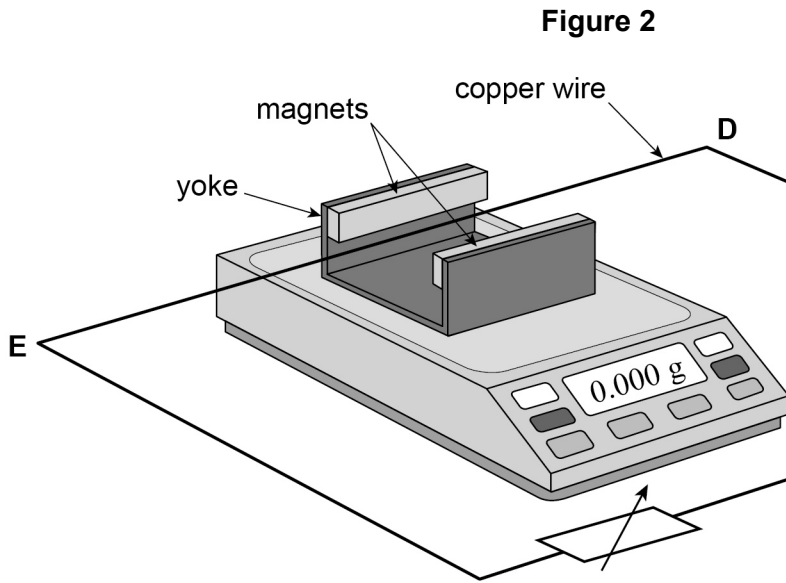
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ANSWER IN THE SPACES PROVIDED**

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0 2

Figure 2 shows two magnets, supported on a yoke, placed on an electronic balance.



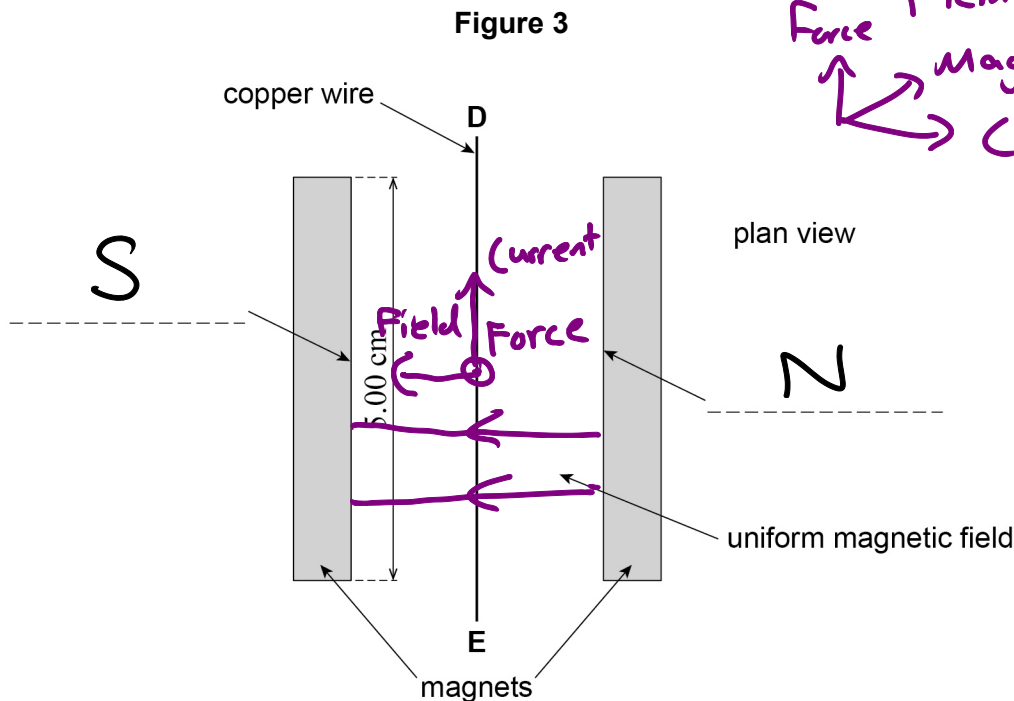
yoke is applying extra force downwards onto the balance.

Wire must feel a force, since current

within magnetic force. yoke feels equal and opposite force to wire

The magnets produce a uniform horizontal magnetic field in the region between them. A copper wire DE is connected in the circuit shown in Figure 2 and is clamped horizontally at right angles to the magnetic field.

Figure 3 shows a simplified plan view of the copper wire and magnets.



Left hand rule: Force Fleming Magnetic Field Current

When the apparatus is assembled with the switch open, the reading on the electronic balance is set to 0.000 g. This reading changes to a positive value when the switch is closed.



0 2 . 1

Which of the following correctly describes the **direction of the force** acting on the wire **DE** due to the magnetic field when the switch is **closed**?

Tick (✓) the correct box.

[1 mark]

towards the left magnet in **Figure 3**

towards the right magnet in **Figure 3**

vertically up

vertically down

yoke pushed downwards, by Newton's 3rd law wire is pulled upwards.

0 2 . 2

Label the **poles of the magnets** by putting **N** or **S** on each of the two dashed lines in **Figure 3**.

[1 mark]

0 2 . 3

Define the tesla.

$F = BIL$ → length inside magnetic flux density.
 $1N = 1T \times 1A \times 1m$

[1 mark]

$1T$ is the magnetic flux density for which a wire of length $1m$ carrying a current $1A$ experiences a force of $1N$, when the current is perpendicular to the field.

$F = BIL \sin \theta$
 θ angle

0 2 . 4

The magnets are **5.00 cm** long. When the current in the wire is **3.43 A** the reading on the electronic balance is **0.620 g**.

between current and field
 $\sin 90^\circ = 1$

Assume the field is **uniform** and is **zero beyond the length of the magnets**.

$F = mg$ (what balance does)

Calculate the **magnetic flux density** between the magnets.

[2 marks]

$F = BIL \sin \theta, \theta = 90^\circ, \sin \theta = 1$

$F = BIL$

Force received by balance

$B = \frac{F}{IL}$

$F = 0.620 \times 10^{-3} \times 9.81$

$B = \frac{0.620 \times 10^{-3} \times 9.81}{3.43 \times 0.05} \rightarrow cm \rightarrow m$

(same as the force on wire in magnitude)

magnetic flux density = 0.0355 T (3s.f.)

5

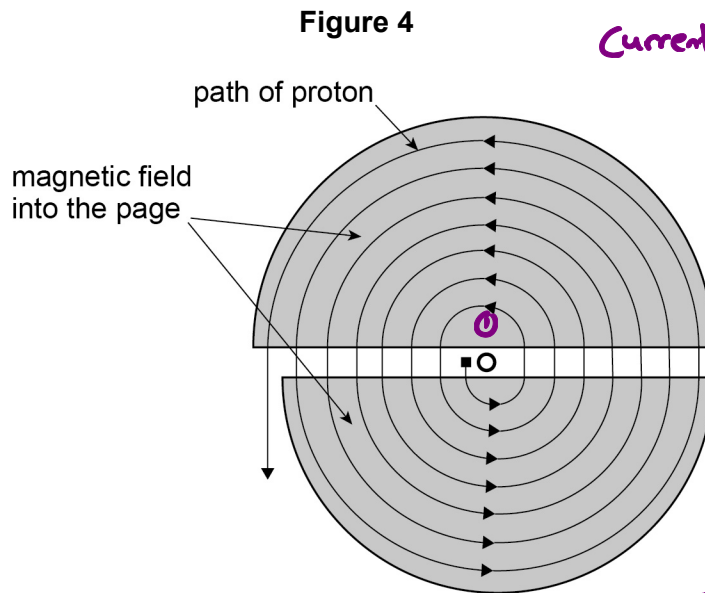
$B = 0.0354647 \dots$ Turn over ▶



0 3

A cyclotron has two D-shaped regions where the magnetic flux density is constant. The D-shaped regions are separated by a small gap. An alternating electric field between the D-shaped regions accelerates charged particles. The magnetic field causes the charged particles to follow a circular path.

Figure 4 shows the path followed by a proton that starts from O.



Fleming's
Current ← ⊗ Flux →
Force ↓ ⊙

So force
v ← ⊙ perpendicular
to velocity
F ↓

For speed to
change:

$$\frac{1}{2}mv^2 \text{ changes}$$

Must do work: apply force over a distance *

0 3 . 1

Explain why it is **not** possible for the magnetic field to alter the speed of a proton while it is in one of the D-shaped regions.

[1 mark]

The magnetic force is perpendicular to the direction of the proton's velocity, so it cannot do any work on the proton and thus cannot change its speed.

* Force must be applied with a component in the direction of motion for work done.



0 3 . 2

Derive an expression to show that the time taken by a proton to travel round one semi-circular path is independent of the radius of the path.

[3 marks]

- Moving under a magnetic flux density $\Rightarrow F = Bq v \sin \theta$ ($q = e$), $\theta = 90^\circ$, $F = Bev$
 - Circular motion $F = \frac{mv^2}{r}$, $v = \omega r$, $\omega = \frac{\theta}{t}$

Circular motion + under magnetic field

$$Bev = \frac{mv^2}{r} \rightarrow v = \frac{Ber}{m}$$

$$v = \omega r, \omega = \frac{\pi}{t} \rightarrow v = \frac{\pi r}{t}$$

time taken \rightarrow to move round semi-circle

$$\frac{Ber}{m} = \frac{\pi r}{t} \rightarrow t = \frac{\pi m}{Be}$$

Independent of r

0 3 . 3

The maximum radius of the path followed by the proton is 0.55 m and the magnetic flux density of the uniform field is 0.44 T.

Ignore any relativistic effects.

we knew proton mass

Calculate the maximum speed of a proton when it leaves the cyclotron.

maximum speed is [2 marks]

$$v = \frac{Ber}{m}$$

at maximum radius ($v \propto r$)

$$\text{maximum speed } v = \frac{0.44 \times 1.60 \times 10^{-19} \times 0.55}{1.673 \times 10^{-27}}$$

\uparrow proton mass

$$v = 2.3144 \dots \times 10^7$$

$$\approx 2.3 \times 10^7$$

maximum speed = 2.3×10^7 m s⁻¹ (2 s.f.)

6

Turn over ►



0 4

The core of a thermal nuclear reactor contains a number of components that are exposed to moving neutrons.

0 4 . 1

State what happens to a neutron that is incident on the moderator.

[1 mark]

The neutron collides with atoms in the moderator and loses speed.

0 4 . 2

State what happens to a neutron that is incident on a control rod.

[1 mark]

The neutron is absorbed.

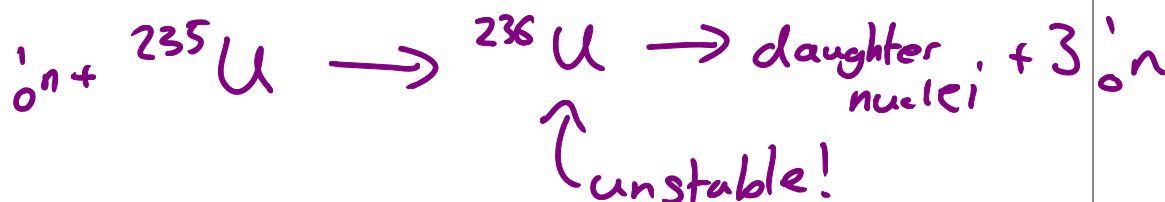
0 4 . 3

A slow-moving neutron is in collision with a nucleus of an atom of the fuel which causes fission.

Describe what happens in the process.

[3 marks]

The neutron is absorbed, causing the uranium nucleus to decay into daughter nuclei, as well as into several neutrons.



0 4 . 4

A thermal nuclear reactor produces radioactive waste.

State the source of this waste and discuss some of the problems faced in dealing with the waste at various stages of its treatment.

Your answer should include:

- the main source of the most dangerous waste
- a brief outline of how waste is treated
- problems faced in dealing with the waste, with suggestions for overcoming these problems.

[6 marks]

The source of the waste is the radioactive daughter nuclei from fission of uranium-235. In treatment, first the waste is cooled in ponds (or other sources of water). Then, the plutonium/uranium are separated, before the high level waste is vitrified (made into solid glass). This is then placed in lead barrels and stored deep underground. During treatment, several problems are encountered. Firstly, the waste is very hot when removed from the reactor and so is cooled in water. Secondly, to prevent the high level waste from leaking, it is vitrified. Finally, the waste is put into lead containers since this attenuates the radiation it produces.

2 marks from here (treatment process)

3 marks from here (problems/solutions)

NB: Only 2 spelling/grammatical errors allowed otherwise marks are deducted.

Extra space is available on the next page if needed

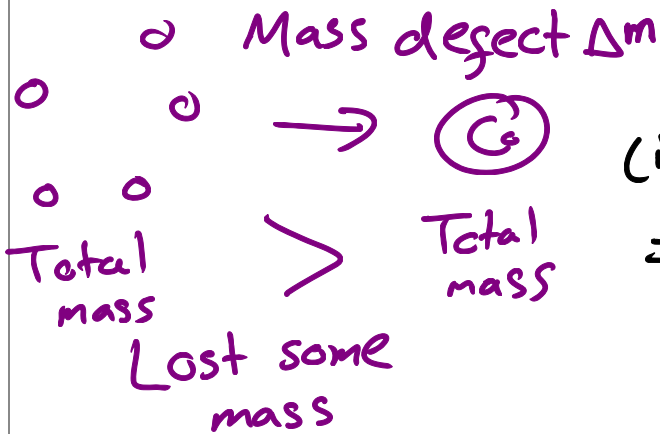
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0 5 . 1

Calculate the binding energy, in MeV, of a nucleus of $^{59}_{27}\text{Co}$.nuclear mass of $^{59}_{27}\text{Co} = 58.93320 \text{ u} \rightarrow \text{amu}$

[3 marks]



Mass of nucleons
(in amu)
(protons)

$$= 27 \times 1.00728$$

$$+ (59 - 27) \times 1.00867$$

$$= 59.474 \text{ u}$$

Mass defect $\Delta m =$

$$59.474 - 58.93320 = 0.5408 \text{ u}$$

1 u is equivalent to 931.5 MeV

$\rightarrow 4 \text{ s.f.}$

$$\Delta E = \Delta mc^2$$

binding energy

$$\Delta E = \Delta m \text{ in u} \times 931.5 \text{ MeV} = 931.5 \times \Delta m \text{ MeV}$$

$$\Delta E = 931.5 \times 0.5408 = 503.7552$$

binding energy = 503.8 MeV (4 s.f.)

Turn over ►

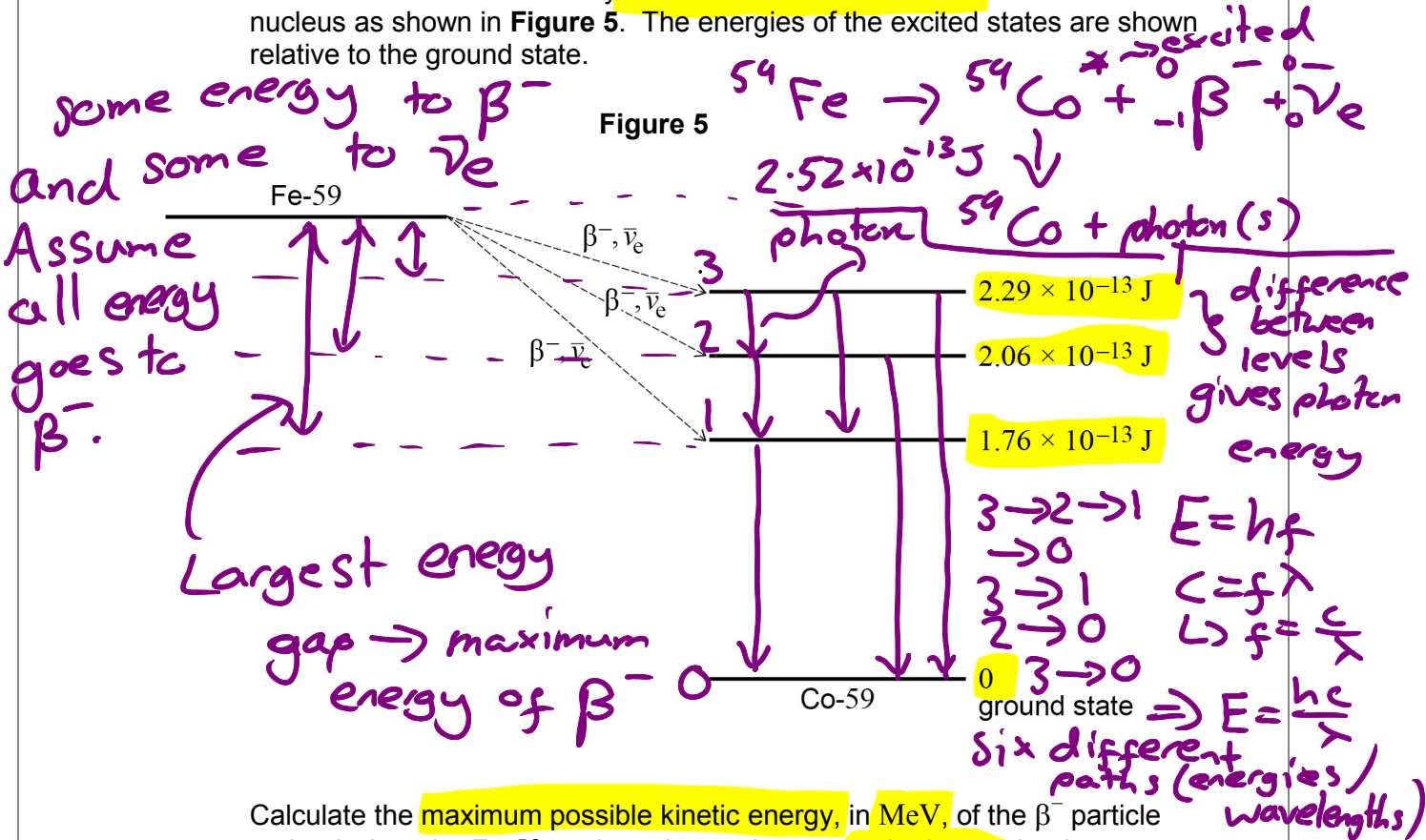


0 5 . 2

A nucleus of iron Fe-59 decays into a stable nucleus of cobalt Co-59. It decays by β^- emission followed by the emission of γ -radiation as the Co-59 nucleus de-excites into its ground state.

The total energy released when the Fe-59 nucleus decays is 2.52×10^{-13} J.

The Fe-59 nucleus can decay to one of three excited states of the cobalt-59 nucleus as shown in Figure 5. The energies of the excited states are shown relative to the ground state.



Calculate the maximum possible kinetic energy, in MeV, of the β^- particle emitted when the Fe-59 nucleus decays into an excited state that has energy above the ground state.

[2 marks]

Energy difference between the Fe-59 and lowest excited state

$$\Delta E = 2.52 \times 10^{-13} - 1.76 \times 10^{-13}$$

$$= 0.76 \times 10^{-13} \text{ J}$$

$1 \text{ eV} = 1.60 \times 10^{-19} \text{ J}$

Convert to MeV:

$$\frac{\Delta E}{1.60 \times 10^{-19} \times 10^6} = \frac{0.76 \times 10^{-13}}{1.60 \times 10^{-19} \times 10^6} = 0.475 \text{ MeV}$$

maximum kinetic energy = 0.48 MeV (2s.f.)



0 5 . 3

Following the production of excited states of $^{59}_{27}\text{Co}$, γ -radiation of discrete wavelengths is emitted.

State the maximum number of discrete wavelengths that could be emitted.

[1 mark]

maximum number = 6

0 5 . 4

Calculate the longest wavelength of the emitted γ -radiation.

[3 marks]

$$E = \frac{hc}{\lambda} \quad \text{Longest wavelength} \Rightarrow \text{lowest energy.}$$

Smallest energy difference is between levels 3 and 2.

$$\text{Therefore } E = 2.29 \times 10^{-13} - 2.06 \times 10^{-13} \\ = 0.23 \times 10^{-13} \text{ J}$$

$$E = \frac{hc}{\lambda} \rightarrow \lambda = \frac{hc}{E} = \frac{6.63 \times 10^{-34} \times 3 \times 10^8}{0.23 \times 10^{-13}} \\ = 8.649593 \dots \times 10^{-12}$$

longest wavelength = 8.65×10^{-12} m

9

(3 s.f.)

Turn over ►



0 6 . 1

State what is represented by gravitational field lines.

[1 mark]

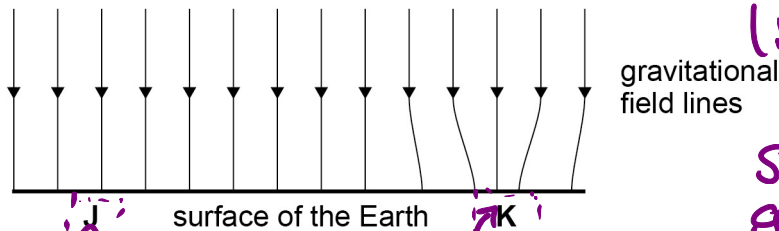
Gravitational field lines represent the direction and relative size of the force acting upon an object with mass in a gravitational field.

following field line
massive object
density of lines
strength of force

0 6 . 2

Figure 6 shows the gravitational field above a small horizontal region on the surface of the Earth.

Figure 6



Denser field lines → stronger field
source of gravitational field is mass
⇒ more mass

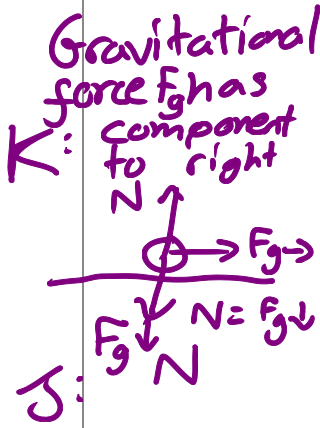
Suggest why the field lines converge over a small area at K.

[2 marks]

Since field lines at K are closer together, the field is stronger. Therefore the material at K has a higher density than the surrounding material.

less dense

(denser (mass))



0 6 . 3

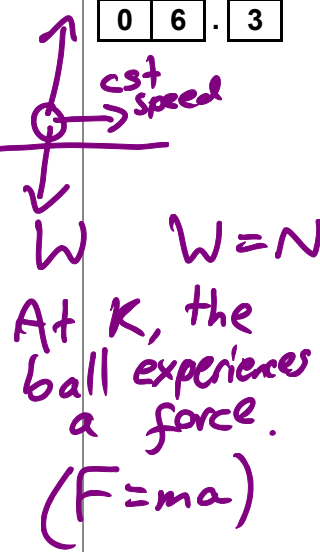
A ball travelling at constant speed passes position J moving towards position K in Figure 6.

Assume friction is negligible.

Explain any change in the speed of the ball as it approaches K.

[2 marks]

The ball accelerates and increases its speed, since there is a component of the gravitational force acting to the right.



Forces at K: vertically balanced, unbalanced force to right.



0 6 . 4

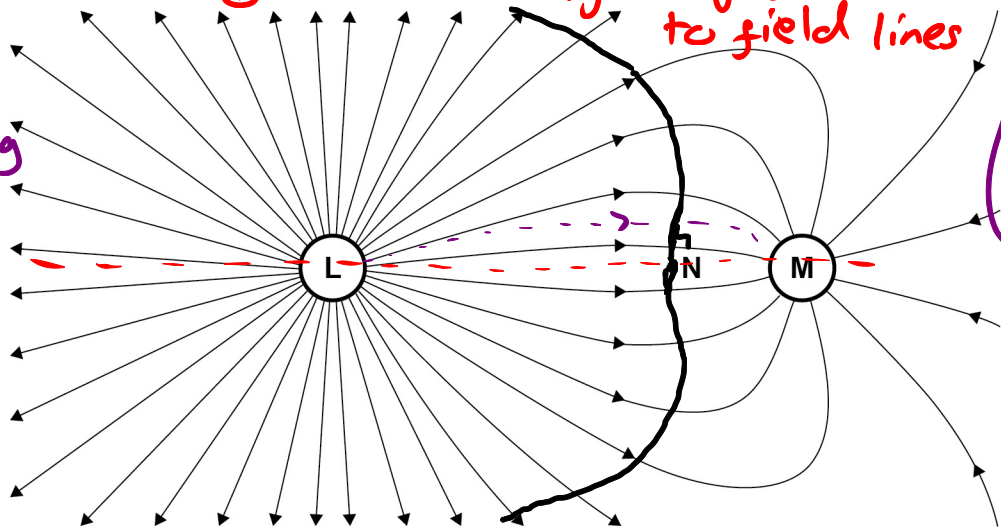
Figure 7 shows lines of force for the electric field surrounding two charged objects L and M.

Criteria:

Line had to bend to the left.
Line is symmetrical about 1 [Line at right angles to field lines]

Gravity attracts only.

Field lines leaving L
Field lines are more dense around L



Object repelled
Field lines cannot flow out of object

Equipotential: Part of space where potential is constant

Field Lines show gradient of potential.

Explain why the lines of force shown in Figure 7 cannot represent a gravitational field.

[1 mark]

Lines of gravitational force must always point into a massive object

0 6 . 5

State which object L or M has a charge with the greater magnitude.

E field lines represent direction a small, positive test charge moves

Larger magnitude charge object L
force of larger magnitude

State which object L or M has a positive charge.

+ve - repel other +ve charges so leave object
-ve - attract +ve charges (enter object)
object L

[1 mark]

0 6 . 6

Draw, on Figure 7, an equipotential line that passes through point N. Do not extend your line beyond the given field lines.

* This comes from the direction of the electric force, since the electric force causes motion in the direction of the electric field.

[2 marks]

9

Turn over ►

0 7 . 1

Derive an expression to show that for satellites in a circular orbit

$$T^2 \propto r^3$$

where T is the period of orbit and r is the radius of the orbit.

[2 marks]

Satellites orbit under gravitational force $F = \frac{GMm}{r^2}$



Eliminate F , get two eqns including $v, r,$ and T

Circular orbits: - Centripetal force $F = \frac{mv^2}{r}$

- $v = \frac{2\pi r}{T}$ → radius of orbit
→ time taken to orbit



gravitational force $\frac{GMm}{r^2} = \frac{mv^2}{r}$ → $v^2 = \frac{GM}{r}$

circular motion $v = \frac{2\pi r}{T}$ → $(\frac{2\pi r}{T})^2 = \frac{GM}{r}$

⇒ $T^2 \times GM = 4\pi^2 r^3$
 $T^2 = (\frac{4\pi^2}{GM}) r^3$ ($\frac{4\pi^2}{GM}$ is constant) → $T^2 \propto r^3$

0 7 . 2

Pluto is a dwarf planet. The mean orbital radius of Pluto around the Sun is 5.91×10^9 km compared to a mean orbital radius of 1.50×10^8 km for the Earth.

Calculate in years the orbital period of Pluto.

[2 marks]

(S)

Earth: $T_e^2 = \frac{4\pi^2}{GM} r_e^3$

Pluto: $T_p^2 = \frac{4\pi^2}{GM} r_p^3$

$\frac{T_p^2}{T_e^2} = \frac{4\pi^2}{GM} \frac{r_p^3}{\frac{4\pi^2}{GM} r_e^3}$

$(\frac{T_p}{T_e})^2 = (\frac{r_p}{r_e})^3$

$T_e = 1 \text{ year}$

$(T^2 = (\frac{4\pi^2}{GM}) r^3)$

don't know the mass of the sun

$T_p^2 = (\frac{r_p}{r_e})^3 \times (1 \text{ yr})^2$

$T_p = (\frac{r_p}{r_e})^{3/2} \times 1 \text{ yr}$

$T_p = (\frac{5.91 \times 10^9 \text{ km}}{1.50 \times 10^8 \text{ km}})^{3/2} \times 1 \text{ yr}$

$T_p = 247.3 \dots \text{ yr}$

orbital period of Pluto = 247 yr (3s.f.)



0 7 . 3

A small mass released from rest just above the surface of Pluto has an acceleration of 0.617 m s^{-2} .

Assume Pluto has no atmosphere that could provide any resistance to motion.

Calculate the mass of Pluto. M

(no air resistance)

Give your answer to an appropriate number of significant figures.

radius of Pluto = $1.19 \times 10^6 \text{ m}$

Gravitational Force or potential

$$F = \frac{GMm}{r^2}$$

small mass

[3 marks]



G to 3s.f.

acceleration $F=ma?$ → Force

$$F = ma$$

$$ma = \frac{GMm}{r^2}$$

$$a = \frac{GM}{r^2}$$

$$M = \frac{ar^2}{G} = \frac{0.617 \times (1.19 \times 10^6)^2}{6.67 \times 10^{-11}}$$

$M = 1.3099455 \dots \times 10^{22} \text{ kg}$ mass of Pluto = $1.31 \times 10^{22} \text{ kg}$ (3s.f.)

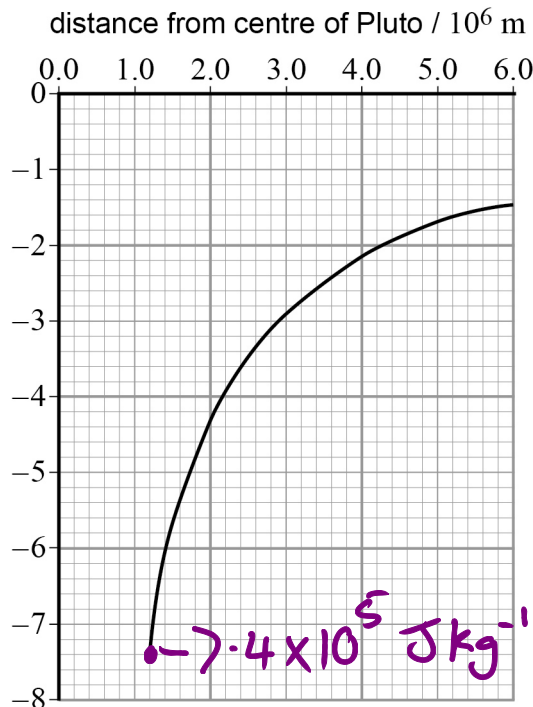
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0 7 . 4

Figure 8 shows the variation in gravitational potential with distance from the centre of Pluto for points at and above its surface.

Figure 8



enough
To escape, kinetic energy must be converted into potential energy such that there is enough gravitational potential energy has increased V_p from a negative value to zero.

note: if there's less E_k than the value of E_p , can't escape.

0 escaped from pluto, no gravitational potential energy

A meteorite hits Pluto and ejects a lump of ice from the surface that travels vertically at an initial speed of 1400 m s^{-1} .

Determine whether this lump of ice can escape from Pluto.

[3 marks]

$E_k, E_p, E_k = \frac{1}{2} m v^2, E_p$ from graph above.

$E_p = V_p \times m$

↑ Lump at pluto surface
 $E_k, E_p < 0$

kinetic energy:
 $E_k = \frac{1}{2} \times m \times (1400)^2 = 9.8 \times 10^5 \times m$

energy needed to escape: $E_p = +7.4 \times 10^5 \times m$
 $9.8 \times 10^5 \times m > 7.4 \times 10^5 \times m$

Yes, the lump can escape pluto as it has enough kinetic energy to escape.

10

END OF SECTION A



Section B

Each of Questions 8 to 32 is followed by four responses, A, B, C and D.

For each question select the best response.

Only **one** answer per question is allowed.

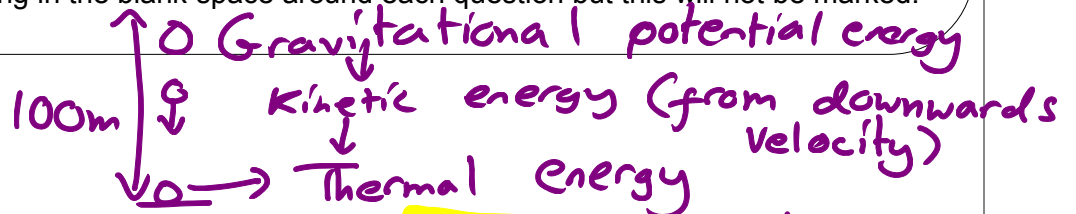
For each answer completely fill in the circle alongside the appropriate answer.

CORRECT METHOD WRONG METHODS

If you want to change your answer you must cross out your original answer as shown.

If you wish to return to an answer previously crossed out, ring the answer you now wish to select as shown.

You may do your working in the blank space around each question but this will not be marked.



0 8

A continuous stream of water falls through a vertical distance of 100 m. Assume no thermal energy is transferred to the surroundings. The specific heat capacity of water is 4200 J kg⁻¹ K⁻¹.

What is the temperature difference of the water between the top and bottom of the waterfall?

Gravitational potential energy = Thermal energy added to a water particle. [1 mark]

- A 0.023 K
- B 0.23 K
- C 2.3 K
- D 4.3 K

Conservation of energy:

$$E_p = mgh = mc\Delta\theta \rightarrow \Delta\theta = \frac{mgh}{mc} = \frac{gh}{c}$$

energy gain of a substance if heated through $\Delta\theta$

$$\Delta\theta = \frac{9.81 \times 100}{4200} = 0.23357... \approx 0.23 K$$

Turn over ►



0 9

A student measures the power of a microwave oven. He places 200 g of water at 23 °C into the microwave and heats it on full power for 1 minute. When he removes it, the temperature of the water is 79 °C.

The specific heat capacity of water is 4200 J kg⁻¹ K⁻¹.

What is the average rate at which thermal energy is gained by the water?

[1 mark]

- A 780 W
- B 840 W
- C 1.1 kW
- D 4.6 kW

$$P = \frac{E}{t}, E = mc\Delta\theta$$

$$E = 200 \times 10^{-3} \times 4200 \times (79 - 23)$$

$$P = \frac{200 \times 10^{-3} \times 4200 \times 56}{1 \times 60}$$

$$P = 784 \text{ W}$$

A
 B
 C
 D

1 0

The composition of a carbon dioxide (CO₂) molecule is one atom of ¹²₆C and two atoms of ¹⁶₈O.

$$\text{Mass of one CO}_2 = 12u + 2 \times 16u$$

What is the number of molecules of CO₂ in 2.2 kg of the gas?

[1 mark]

- A 1.0 × 10²²
- B 3.0 × 10²²
- C 3.0 × 10²⁵
- D 4.7 × 10²⁵

$$\text{Number of molecules} = \frac{\text{total mass}}{\text{mass of one molecules}}$$

$$N = \frac{m}{44u} = \frac{2.2}{44 \times 1.661 \times 10^{-27}}$$

$$N = 3.010 \dots \times 10^{25} \approx 3.0 \times 10^{25}$$

A
 B
 C
 D

1 1

What is the total internal energy of 2.4 mol of an ideal gas which has a temperature of 15 °C?

[1 mark]

- A 6.0 × 10⁻²¹ J
- B 1.4 × 10⁻²⁰ J
- C 4.5 × 10² J
- D 8.6 × 10³ J

Total internal energy is sum of randomly distributed kinetic + potential energies.

Average energy of one gas particle × number of gas particles = Total internal energy.

A
 B
 C
 D

$$E_{\text{total}} = 8.616 \dots \times 10^3 \text{ J} \approx 8.6 \times 10^3 \text{ J}$$

T = 15 + 273
 ↑ convert into K.

Ideal → interactions between particles are negligible except during collisions → no potential energy.

→ Only energy is kinetic. $E_{\text{one}} = \frac{3}{2} k_B T$, $N = n N_A$
 $E_{\text{total}} = n N_A \times \frac{3}{2} k_B T = 2.4 \times 6.022 \times 10^{23} \times \frac{3}{2} \times 1.38 \times 10^{-23} \times T$



$$g = \frac{GM}{r^2}$$

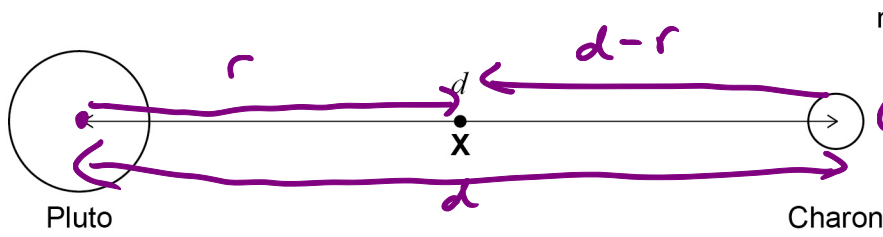
$$g_{\text{pluto}} - g_{\text{charon}} = 0 = \frac{GM_p}{r^2} - \frac{GM_c}{(d-r)^2}, M_c = \frac{1}{9}M_p$$

Do not write outside the box

1 2

Charon is a moon of Pluto that has a mass equal to $\frac{1}{9}$ that of Pluto.

The distance between the centre of Pluto and the centre of Charon is d . X is the point at which the resultant gravitational field due to Pluto and Charon is zero.



not to scale

$$0 = GM_p \left(\frac{1}{r^2} - \frac{1}{9} \frac{1}{(d-r)^2} \right)$$

$$\frac{1}{9} \frac{1}{(d-r)^2} = \frac{1}{r^2}$$

$$r^2 = 9(d-r)^2$$

What is the distance of X from the centre of Pluto?

[1 mark]

- A $\frac{2}{9}d$
- B $\frac{2}{3}d$
- C $\frac{3}{4}d$
- D $\frac{8}{9}d$

$$r = \pm 3(d-r)$$

either

$$+ : r = 3d - 3r$$

$$4r = 3d$$

$$r = \frac{3d}{4} \checkmark$$

$$- : r = -3d + 3r$$

$$-2r = -3d$$

$$r = \frac{3d}{2} \times$$

1 3

The distance between the Sun and Mars varies from $2.1 \times 10^{11} \text{ m}$ to $2.5 \times 10^{11} \text{ m}$.

When Mars is closest to the Sun, the force of gravitational attraction between them is F .

What is the force of gravitational attraction between them when they are furthest apart?

[1 mark]

- A $0.71F$
- B $0.84F$
- C $1.2F$
- D $1.4F$

$$F = \frac{GMm}{r^2}$$

no masses
force and distance

$$F \propto \frac{1}{r^2}$$

near: (n) $F_n = \frac{GMm}{r_n^2}$

far: (f) $F_f = \frac{GMm}{r_f^2}$

$$\frac{F_f}{F_n} = \frac{\left(\frac{2.1 \times 10^{11}}{2.5 \times 10^{11}} \right)^2}{1} = \frac{2.1}{2.5}$$

$$\frac{F_f}{F_n} = \frac{GMm}{r_f^2} = \frac{r_n^2}{r_f^2} = \left(\frac{r_n}{r_f} \right)^2 = \left(\frac{2.1}{2.5} \right)^2$$

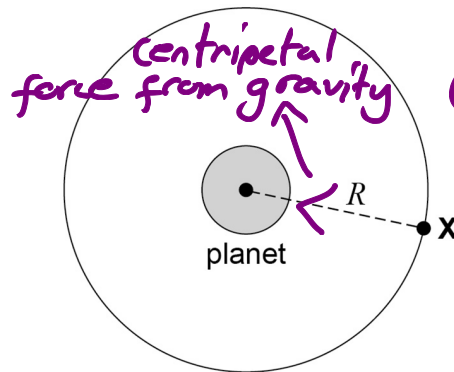
NB: omit 10¹¹ since the units are the same and divide either



Turn over

1 4

A satellite X of mass m is in a concentric circular orbit of radius R about a planet of mass M .



- Circular orbit $\frac{mv^2}{R}$
 (Centripetal force / Circular motion)
 - Gravitational force $\frac{GMm}{R^2}$
 - Kinetic energy is goal $\rightarrow E_k = \frac{1}{2}mv^2$

What is the kinetic energy of X?

E_k contains v ,

[1 mark]

A $\frac{GMm}{2R}$

B $\frac{GMm}{R}$

C $\frac{2GMm}{R}$

D $\frac{4GMm}{R}$

must use centripetal force
 $=$ gravitational force to
 get an equation for v .

$$\frac{mv^2}{R} = \frac{GMm}{R^2}$$

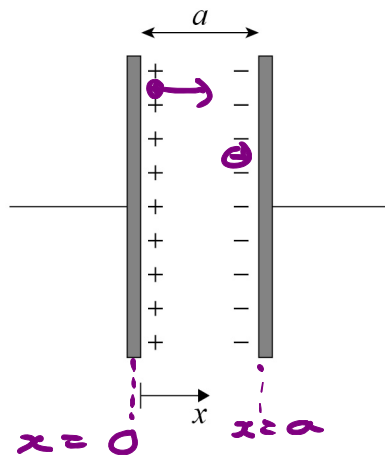
$$v^2 = \frac{GM}{R}$$

$$E_k = \frac{1}{2} m v^2 = \frac{1}{2} m \frac{GM}{R} = \frac{GMm}{2R}$$



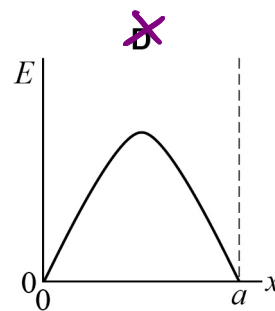
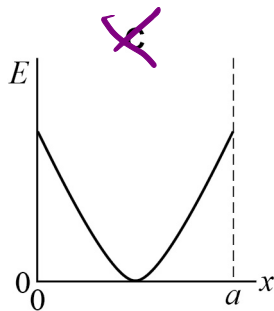
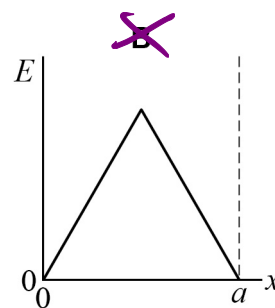
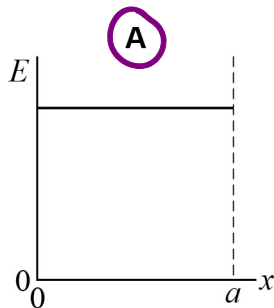
1 5

Two parallel metal plates of separation a carry equal and opposite charges.



Which graph best represents how the electric field strength E varies with the distance x in the space between the two plates?

[1 mark]



B, D out (since field is zero at plates)

- A
- B
- C
- D

Turn over ►



1 | 6

A particle of mass m and charge q is accelerated through a potential difference V over a distance d .

What is the average acceleration of the particle?

[1 mark]

A $\frac{qV}{md}$

B $\frac{mV}{qd}$

C $\frac{V}{mqd}$

D $\frac{dV}{mq}$

$F = ma, E = \frac{V}{d}$
 Electric force
 $F = qE$
 $= \frac{qV}{d}$ only force is electric
 $\frac{qV}{d} = ma$
 $a = \frac{qV}{md}$

1 | 7

An electron moves through a distance of 0.10 m parallel to the field lines of a uniform electric field of strength 2.0 kN C^{-1} .

What is the work done on the electron?

Work done

[1 mark]

A zero

B $1.6 \times 10^{-17} \text{ J}$

C $3.2 \times 10^{-17} \text{ J}$

D $1.6 \times 10^{-21} \text{ J}$

$\leftarrow e^-$ as parallel to field lines.
 $W = QV, Q = e$
 Uniform field:
 $E = \frac{V}{d}$
 $V = Ed$
 $W = QEd$ $\text{KN} \rightarrow \text{N}$
 $W = eEd = 1.60 \times 10^{-19} \times 2 \times 10^3 \times 0.1$
 $= 3.20 \times 10^{-17} \text{ J}$



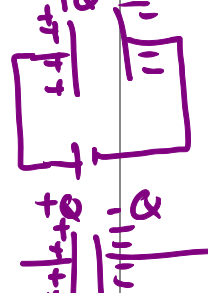
1 | 8

A parallel-plate capacitor is fully charged and then disconnected from the power supply. A dielectric is then inserted between the plates.

Which row correctly identifies the charge on the plates and the electric field strength between the plates?

Dielectric has larger $\epsilon_r \uparrow$:
 $C = \frac{\epsilon_0 \epsilon_r A}{d}$
 ϵ_r - relative permittivity.
 Larger ϵ_r smaller electric field for the same

$(E = V/d)$
 $V = Ed$

Charge: $-Q$
 [1 mark]

 Charge has to remain the same

	Charge		Electric field strength	
A	Stays the same ✓		Increases	<input checked="" type="checkbox"/>
B	Increases	x	Decreases	<input checked="" type="checkbox"/>
C	Increases	x	Increases	<input checked="" type="checkbox"/>
D	Stays the same ✓		Decreases	<input checked="" type="checkbox"/>

amount of charge! $Q = CV$, if $\epsilon_r \uparrow, C \uparrow$, but Q cst so $V \downarrow$

1 | 9

A capacitor of capacitance C has a charge of Q stored on the plates. The potential difference between the plates is doubled.

What is the change in the energy stored by the capacitor?

[1 mark]

- $W = \frac{1}{2} QV$
- A $\frac{Q^2}{2C}$
- B $\frac{Q^2}{C}$
- C $\frac{3Q^2}{2C}$
- D $\frac{2Q^2}{C}$
- $C = \frac{Q}{V}$
 $Q = CV$ $V = \frac{Q}{C}$
 Sub in $W \rightarrow W = \frac{1}{2} CV^2, W = \frac{1}{2} \frac{Q^2}{C}$

Energy originally stored: $W = \frac{1}{2} CV^2$
 (because changing p.d.)

$V \rightarrow 2V$, new energy $W_{new} = \frac{1}{2} C \times (2V)^2 = 2CV^2$

Change in energy: $W_{new} - W = 2CV^2 - \frac{1}{2} CV^2 = \frac{3}{2} CV^2$

Change back to in terms of charge: $Q = CV, V = \frac{Q}{C}$
 change = $\frac{3}{2} \times C \times (\frac{Q}{C})^2 = \frac{3}{2} \frac{Q^2}{C}$

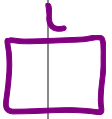
Turn over ▶



2 0

A capacitor consists of two parallel square plates of side l separated by distance d . The capacitance of the arrangement is C .

What is the capacitance of a capacitor with square plates of side $2l$ separated by a distance $\frac{d}{2}$?



- A C
- B $2C$
- C $4C$
- D $8C$

Handwritten solution for Question 20:

Original capacitor: $C = \frac{\epsilon_0 \epsilon_r A}{d}$ where $A = l^2$.
 New capacitor: $C_{new} = \frac{\epsilon_0 \epsilon_r A_{new}}{d_{new}}$ where $A_{new} = (2l)^2 = 4l^2$ and $d_{new} = \frac{d}{2}$.
 $C_{new} = \frac{\epsilon_0 \epsilon_r \times 4l^2}{\frac{d}{2}} = 8 \frac{\epsilon_0 \epsilon_r l^2}{d} = 8C$

Answers: A, B, C, D

2 1

A capacitor of capacitance $120 \mu\text{F}$ is charged and then discharged through a $20 \text{ k}\Omega$ resistor.

What fraction of the original charge remains on the capacitor 4.8 s after the discharge begins?

- A 0.14
- B 0.37
- C 0.63
- D 0.86

Handwritten solution for Question 21:

Discharging: $Q = Q_0 e^{-\frac{t}{RC}}$
 where Q_0 is initial charge.
 $\frac{Q}{Q_0} = e^{-\frac{t}{RC}}$
 where $\frac{Q}{Q_0}$ is fraction of charge.

Calculations:
 $RC = 20 \times 10^3 \times 120 \times 10^{-6} = 2.4 \text{ s}$
 $\frac{t}{RC} = \frac{4.8}{2.4} = 2 \Rightarrow \frac{Q}{Q_0} = e^{-2} = 0.1353 \dots \approx 0.14$

Answers: A, B, C, D



2 2

A coil with 20 circular turns each of diameter 60 mm is placed in a uniform magnetic field of flux density 90 mT.

Initially the plane of the coil is perpendicular to the magnetic field lines as shown in Figure X.

Area (circle)
 $= \pi r^2$
 $= \pi \times \left(\frac{d}{2}\right)^2$
 $= \pi \times \left(\frac{60 \times 10^{-3}}{2}\right)^2$
 mm \rightarrow m

Figure X

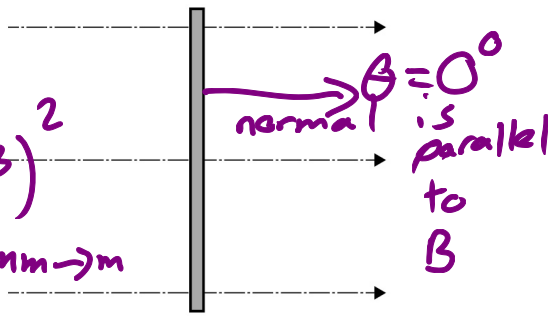
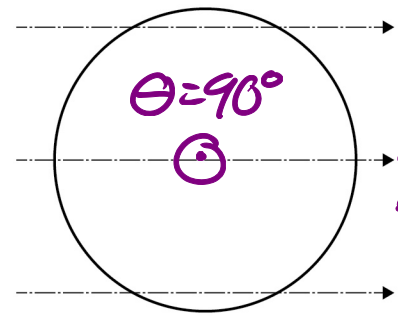


Figure Y



$\vec{L} = N \vec{A}$
 $\mathcal{E} = \frac{\mathcal{E} \Delta(N\phi)}{\Delta t}$
 $\frac{\Delta(N\phi)}{\Delta t} \leftarrow \text{const}$
 $\frac{\Delta \phi}{\Delta t} = \frac{\phi_{\text{end}} - \phi_{\text{start}}}{t_{\text{end}} - t_{\text{start}}}$
 $\mathcal{E} = N \frac{\Delta \phi}{\Delta t}$

The coil is rotated about a vertical axis by 90° in a time of 0.20 s so that its plane becomes parallel to the field lines as shown in Figure Y. Assume that the rate of change of flux linkage remains constant.

What is the emf induced in the coil?

- A zero
- B 1.3 mV
- C 25 mV
- D 100 mV

$\phi = BA \cos \theta$
 θ between normal to area and flux density
 [1 mark]
 start $\cos \theta = 1 \rightarrow$ end $\cos \theta = 0$
 $\phi_{\text{start}} = BA$ $\phi_{\text{end}} = 0$
 $\mathcal{E} = 20 \times \frac{(-1) \times \pi \times \left(\frac{60 \times 10^{-3}}{2}\right)^2 \times 90 \times 10^{-3}}{0.2}$
 $\mathcal{E} = -0.02544 \dots = -25 \text{ mV}$
 magnitude of $\mathcal{E} = 25 \text{ mV}$

2 3

The mean power dissipated in a resistor is 47.5 μW when the root mean square (rms) voltage across the resistor is 150 mV.

What is the peak current in the resistor?

- A 2.3×10^{-4} A
- B 4.5×10^{-4} A
- C 2.3×10^3 A
- D 4.5×10^3 A

$I_0 = 4.4783 \dots \times 10^{-4} \text{ A}$
 $\approx 4.5 \times 10^{-4} \text{ A}$ [1 mark]
 $P = I_{\text{rms}} V_{\text{rms}}$
 $I_{\text{rms}} = \frac{I_0}{\sqrt{2}} \rightarrow$ peak current
 $P = \frac{I_0}{\sqrt{2}} \times V_{\text{rms}}$
 $I_0 = \frac{\sqrt{2} P}{V_{\text{rms}}} = \frac{\sqrt{2} \times 47.5 \times 10^{-6}}{150 \times 10^{-3}}$
 μW \rightarrow W
 Turn over \blacktriangleright



Output power $P = IV \Rightarrow I = \frac{P}{V}$
 Power dissipated in wires $I^2 R = \frac{P^2 R}{V^2}$
 Larger $V \Rightarrow$ power loss in wire decreases.
 $I = \frac{P}{V} \Rightarrow I$ also gets smaller for larger V

2 4

The National Grid is used to transfer electrical energy from power stations to consumers.

What conditions for the transmission voltage and the transmission current give the most efficient transfer of energy through the National Grid?

[1 mark]

	Transmission voltage	Transmission current	
A	High ✓	High ✗	<input type="radio"/>
B	High ✓	Low ✓	<input checked="" type="radio"/>
C	Low ✗	High	<input type="radio"/>
D	Low ✗	Low	<input type="radio"/>

2 5

A mains transformer has a primary coil of 2500 turns and a secondary coil of 130 turns. The primary coil is connected to a mains supply where V_{rms} is 230 V. The secondary coil is connected to a lamp of resistance 6.0 Ω . The transformer is 100% efficient.

What is the peak power dissipated in the lamp?

[1 mark]

- A 12 W
- B 24 W
- C 48 W
- D 96 W

Voltage across secondary coil:

$$\frac{N_p}{N_s} = \frac{V_{p,rms}}{V_{s,rms}}$$

$$V_{s,rms} = V_{p,rms} \times \frac{N_s}{N_p}$$

$$V_{s,rms} = 230 \times \frac{130}{2500} = 11.96 \text{ V}$$

$$P_{peak} = I_{o,s} V_{o,s} = \frac{V_{o,s}^2}{R} = \frac{2}{R} V_{s,rms}^2 = \frac{2}{6} \times 11.96^2 = 47.6805 \dots \text{ W}$$

$V_{p,rms} = \frac{V_{p,o}}{\sqrt{2}}$
 $\left(\frac{V_{p,o}}{V_{s,o}} = \frac{V_{p,rms}}{V_{s,rms}}\right)$
 $V_{s,rms} = \frac{V_{s,o}}{\sqrt{2}}$
 $V_{s,o} = \sqrt{2} V_{s,rms}$

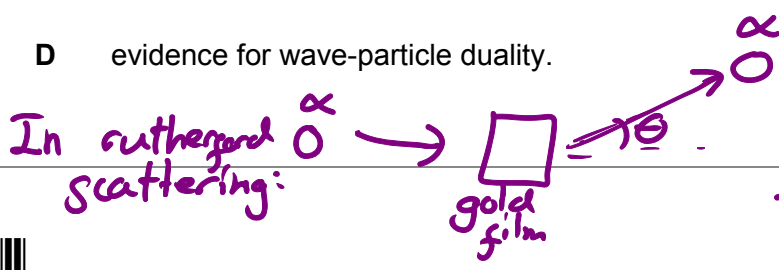
2 6

The Rutherford scattering experiment led to

[1 mark]

- A the discovery of the electron.
- B the quark model of hadrons.
- C the discovery of the nucleus.
- D evidence for wave-particle duality.

Atom is empty space with positive nucleus at centre \Rightarrow C



- Most particles are undeflected
- Some particles deflected by a small angle
- Some reflected at 180°



2 | 7

A Geiger counter is placed near a radioactive source and different materials are placed between the source and the Geiger counter.

The results of the tests are shown in the table.

Material	Count rate of Geiger counter / s ⁻¹
None	1000
Paper	unchanged. 1000 ⇒ no α
Aluminium foil	↓ 250 ⇒ β
Thick steel	↓ 1000 → 50 ⇒ γ

α (He nucleus)
 2+
 Large mass
 ↓
 α easily absorbed
 β less easily absorbed
 γ much less easily absorbed

β air range (1m)
 → absorbed by Al

e⁻
 mass is much smaller than α
 ±1

no mass, uncharged, need dense/thick material (steel, lead)

What is the radiation emitted by the source?

[1 mark]

- A α only
- B α and γ
- C α and β
- D β and γ

2 | 8

Nobelium-259 has a half-life of 3500 s.

What is the decay constant of nobelium-259?

[1 mark]

- A $8.7 \times 10^{-5} \text{ s}^{-1}$
- B $2.0 \times 10^{-4} \text{ s}^{-1}$
- C $1.7 \times 10^{-2} \text{ s}^{-1}$
- D $1.2 \times 10^{-2} \text{ s}^{-1}$

$T_{1/2}, \lambda$

$T_{1/2} = \frac{1}{\lambda} \ln 2$

$(N = N_0 e^{-\lambda t})$
 $\frac{N}{N_0} = e^{-\lambda t} = \left(\frac{1}{2}\right)^{\frac{t}{T_{1/2}}}$

$\lambda = \frac{1}{T_{1/2}} \ln 2$
 $\lambda = \frac{1}{3500} \times \ln 2$

$\lambda = 1.980... \times 10^{-4} \text{ s}^{-1}$
 $\approx 2.0 \times 10^{-4} \text{ s}^{-1}$

Turn over ►



2 | 9

A pure sample of nuclide X containing N nuclei has an activity A .
The half-life of X is 6000 years.

A pure sample of nuclide Y containing $3N$ nuclei has an activity $6A$.

What is the half-life of nuclide Y?

- A 1000 years
- B 3000 years
- C 12 000 years
- D 18 000 years

$X: A = \lambda_x N \rightarrow \lambda_x = \frac{A}{N}$

Half-life: $T_{\frac{1}{2},x} = \frac{1}{\lambda_x} \ln 2$

$T_{\frac{1}{2}} \propto \frac{1}{\lambda}$

$Y: A_y = 6A = \lambda_y N_y = \lambda_y \times 3N$
 $\rightarrow \lambda_y = \frac{A}{N} \times 2 \rightarrow \lambda_y = 2\lambda_x$

$T_{\frac{1}{2},y} = \frac{6000}{2} = 3000 \text{ years}$

[1 mark]

$T_{\frac{1}{2}} \propto \frac{1}{\lambda}$
 $\lambda_y = 2\lambda_x$
 $T_{\frac{1}{2},y} = \frac{1}{2} T_{\frac{1}{2},x}$
(inversely proportional)

3 | 0

Cobalt-60 has a half-life of 5.27 years. $T_{\frac{1}{2}} = 60 \mu$

What is the total activity of 1.0 g of cobalt-60?

- A 4.2×10^{13} Bq
- B 2.2×10^{14} Bq
- C 2.5×10^{15} Bq
- D 1.3×10^{21} Bq

$A = \lambda N \approx 4.2 \times 10^{13} \text{ Bq}$

$T_{\frac{1}{2}} = \frac{1}{\lambda} \ln 2$
 $\lambda = \frac{1}{T_{\frac{1}{2}}} \ln 2$

[1 mark]

$N = \frac{\text{total mass}}{\text{mass of one Co-60}} = \frac{1 \times 10^{-3} \text{ kg}}{60 \times 1.661 \times 10^{-27}}$

$N = 1.003411... \times 10^{22}$ radioactive nuclei

$\lambda = \frac{\ln 2}{5.27 \times 365 \times 24 \times 60 \times 60} = 4.170693... \times 10^{-9} \text{ s}^{-1}$
in year in a day seconds in an hour

$A = 1.003... \times 10^{22} \times 4.170693... \times 10^{-9} = 4.18598 \times 10^{13}$



3 1

The radius of a nucleus of the iron nuclide ${}^{56}_{27}\text{Fe}$ is 4.35×10^{-15} m.

What is the radius of a nucleus of the uranium nuclide ${}^{238}_{92}\text{U}$?

- A 2.69×10^{-15} m
- B 2.89×10^{-15} m
- C 6.55×10^{-15} m
- D 7.05×10^{-15} m

Two nuclides

$$R = R_0 A^{1/3}$$

$$R_{\text{Fe}} = R_0 A_{\text{Fe}}^{1/3}$$

$$R_{\text{U}} = R_0 A_{\text{U}}^{1/3}$$

$$\frac{R_{\text{U}}}{R_{\text{Fe}}} = \frac{R_0 A_{\text{U}}^{1/3}}{R_0 A_{\text{Fe}}^{1/3}} = \left(\frac{A_{\text{U}}}{A_{\text{Fe}}}\right)^{1/3}$$

$R_{\text{U}} \approx 7.05 \times 10^{-15}$ m [1 mark]

$$R_{\text{U}} = R_{\text{Fe}} \left(\frac{A_{\text{U}}}{A_{\text{Fe}}}\right)^{1/3}$$

$$= 4.35 \times 10^{-15} \times \left(\frac{238}{56}\right)^{1/3}$$

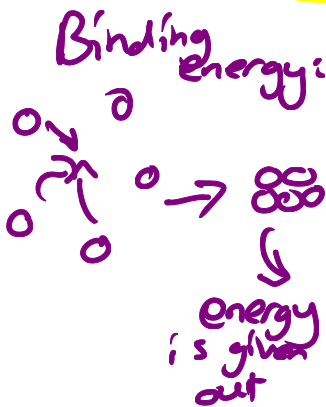
$$= 7.046 \dots \times 10^{-15}$$

3 2

Uranium-236 undergoes nuclear fission to produce barium-144, krypton-89 and three free neutrons.

What is the energy released in this process?

$$\Delta E = E_{\text{After}} - E_{\text{Before}}$$



Nuclide	Binding energy per nucleon / MeV
${}^{236}_{92}\text{U}$	7.5 = B_{U}
${}^{144}_{56}\text{Ba}$	8.3 = B_{B}
${}^{89}_{36}\text{Kr}$	8.6 = B_{K}

[1 mark]

- A 84 MeV
- B 106 MeV
- C 191 MeV
- D 3730 MeV

$$E_{\text{After}} = B_{\text{B}} \times 144 + 89 \times B_{\text{K}} + E_{\text{mass}}$$

$$E_{\text{Before}} = B_{\text{U}} \times 236 + E_{\text{mass}}$$

Before:

236 \rightarrow 92 protons
 $\rightarrow 236 - 92 = 144$ neutrons

After:

56 + 36 protons = 92
 $144 - 56 + 89 - 36 + 3 = 144$ neutrons

END OF QUESTIONS

$$E_{\text{mass}} = \text{number protons} \times m_p + \text{number of neutrons} \times m_n$$

$$\Delta E = 144 \times 8.3 + 89 \times 8.6 + E_{\text{mass}} - (7.5 \times 236 + E_{\text{mass}})$$

$$= 190.6 \text{ MeV}$$



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